

# Capital structure management

Corporate Finance

# Modigliani-Miller (MM)

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- Does capital structure matter?
- Does the value of an asset depend on the mix of debt and equity that is used to finance its purchase?
- Absent taxes, transaction costs or limits, and other frictions, the answer is no
- Obvious in the world of CAPM: asset value depends on its payoffs alone



# The question

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- Consider two corporations with the same random *EBIT* denoted  $X$  over  $t = 1, 2, 3, \dots$
- $Dep = I$  so that unlevered FCFF is  $(1 - \tau)X$
- At first,  $\tau = 0$ , so that unlevered FCFF is  $X$
- First corporation is financed with equity  $E$  and debt  $D$ , its value is:

$$V^L = E + D$$

- L for *levered* or *leverage*
  - Second corporation is 100% equity financed, and has value  $V^U$
- 



# The question

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Can we have:

$$V^L > V^U$$

or

$$V^U > V^L?$$

**MM theorem:** *When markets are perfect,  $V^U = V^L$ .*



# An arbitrage argument

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- Assume, by way of contradiction, that  $V^L > V^U$
- Portfolio 1: Buy fraction  $\alpha$  of levered asset's equity, which costs  $\alpha E$
- Payoff:  $\alpha(X - Dr^D)$
- Portfolio 2: Borrow  $\alpha D$  and buy  $\alpha V^U$  of equity in unlevered firm, which costs:

$$\alpha V^U - \alpha D = \alpha(V^U - D) < \alpha(V^L - D) = \alpha E$$

- Payoff:  $\alpha X - \alpha Dr^D$
  - Violation of the law of one price
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# Return on equity

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- Unlevered case:  $r^U = \frac{X}{V^U}$
- Levered case: 
$$r^E = \frac{(X - r^D D)}{E}$$
$$= r^U + (D/E) (r^U - r^D)$$
- Leverage: more debt means more return on equity as long as  $E(r^U) > r^D$
- What's the catch? Risk goes up:
- $VAR(r^E) = Var(r^U) \left(1 + \frac{D}{E}\right)^2$



# Levered betas

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- How does the beta of the levered firm's equity compare to the beta of the unlevered firm?
- $$\begin{aligned}\beta^L &= \beta(r^E) \\ &= \beta(r^U + (D/E)(r^U - r^D)) \\ &= (1 + (D/E))\beta^U\end{aligned}$$
- It is higher, confirming that leverage implies risk
- Some stake-holders (debt-holders) assume “no” risk leaving equity holders to bear more risk



# Weighted average cost of capital (WACC)

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- $WACC = \frac{E}{E+D} E(r^E) + \frac{D}{E+D} r^D$
- MM proposition II:  $WACC = E(r^U)$  regardless of D
- WACC fact: the asset's value is the expected present value of all future cash flows discounted at the WACC
- Loosely speaking, a positive NPV when discounted at WACC means that cash-flows, in expected terms, are sufficient to meet the expected returns of all stakeholders





# MM: a WACC proof

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Under MM assumptions:

1. Firm cash flows are independent of capital structure
2. Firm value is present value of cash flows at WACC
3. WACC is independent of capital structure

⇒ Firm value is independent of capital structure



# What does MM tell us?

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- Not so much that capital structure does not matter
- It says that if capital structure matters, it must be because of the frictions MM assume away:
  1. Taxes
  2. Costs associated with financial distress
  3. Agency problems (manager incentives vs. shareholder objectives)
  4. ...



# Taxes

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- If asset's owner is a taxed corporation, they face taxes, but debt payments are tax deductible

- FCFF, in each period, is:

$$X - \tau(X - Dr^D) = (1 - \tau)X + \tau Dr^D$$

- The last term is called the tax shield, it adds value to the asset

- One shows:  $V^L = V^U + \tau D$

- General principle:

$$APV = PV(\text{unlevered corporation}) + NPV(\text{financing})$$



# Other MM results with taxes

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- Unlevered case:  $r^U = (1 - \tau)X/V^U$

- Levered case:

1.  $r^E = r^U + \left(\frac{(1-\tau)D}{E}\right)(r^U - r^D)$

2.  $\beta^L = \left(1 + (1 - \tau) \frac{D}{E}\right) \beta^U$

3.  $WACC = \frac{E}{E+D} E(r^E) + \frac{D}{E+D} (1 - \tau)r^D$

- Discounting expected net-of-taxes cash flows at WACC continues to give the right answer

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# WACC issues

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- **WACC has at least two virtues:**
  1. One can write a model (MM) where it is the right discount rate
  2. It has intuitive appeal
  
- **But it relies on heroic assumptions:**
  1. Capital structure is fixed
  2. Discount rates have no term structure
  3. ...



# If debt's so great, why use equity at all?

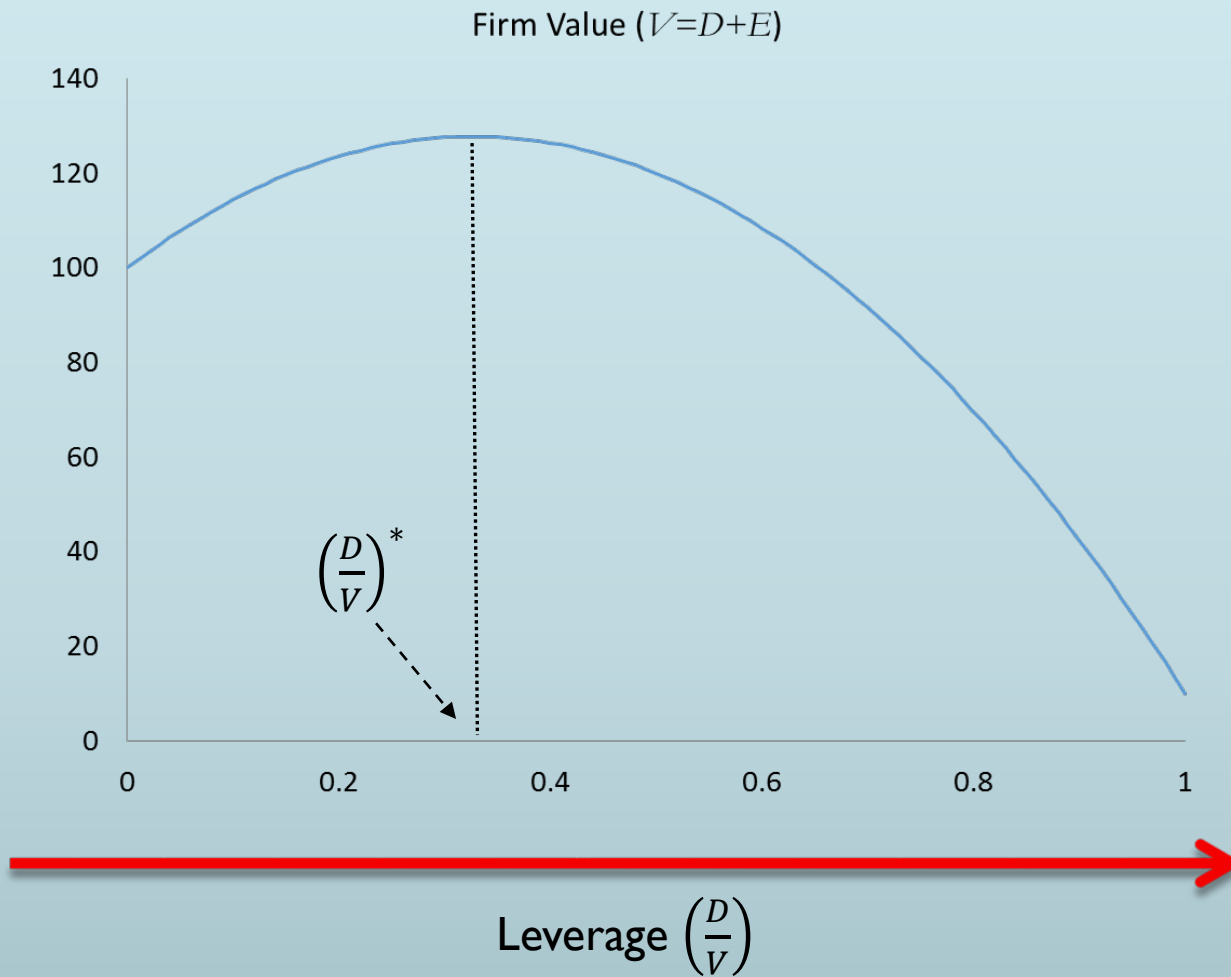
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- MM abstract from issues associated with financial distress
- Distress is costly both for obvious reasons and more subtle ones
- As a result, optimal debt-to-value ratio is less than 100%
- Trade-off theory: optimal capital structure balances the costs and benefits of leverage



# Trade-off theory

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# Trade-off theory, WACC version

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- Consider a corporation with only debt and equity so that:

$$WACC = \frac{E}{D + E} r^E + \frac{D}{D + E} r^D (1 - t)$$

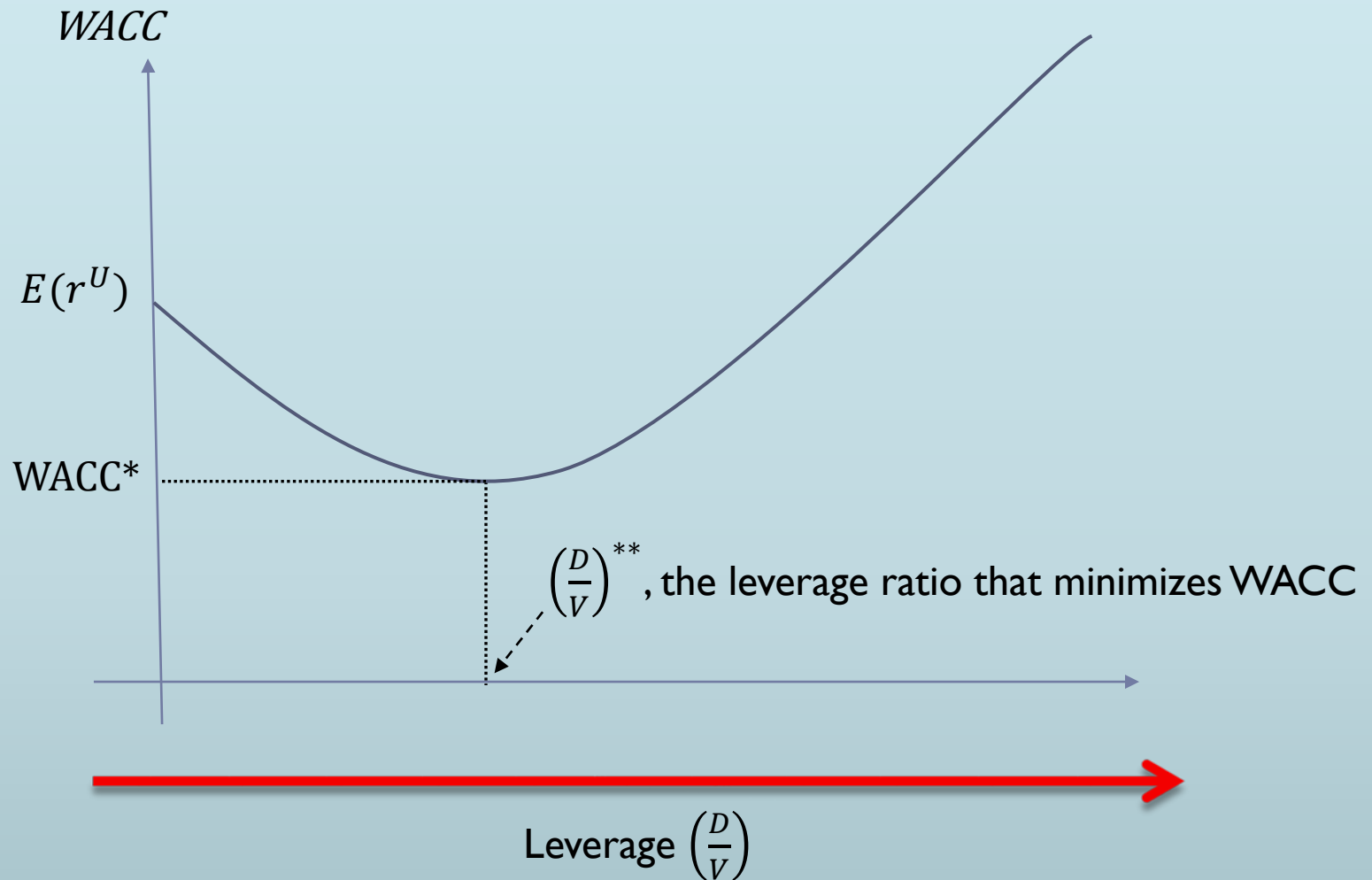
- A treasurer wants to ask weather increasing  $D$  will lower their cost of capital
- Three main effects:
  1. Weight on debt increases (-)
  2.  $r^E$  goes up (+)
  3.  $r^D$  goes up if debt is risky (+)
- Under perfect markets and no taxes, the first two effects exactly cancel one another (**Modigliani-Miller proposition II**)
- With taxes, effect 1 is stronger than effect 2
- With default risk, effect 3 becomes stronger and stronger as  $D$  goes up (it is *convex*, that is)





# Trade-off theory, WACC version

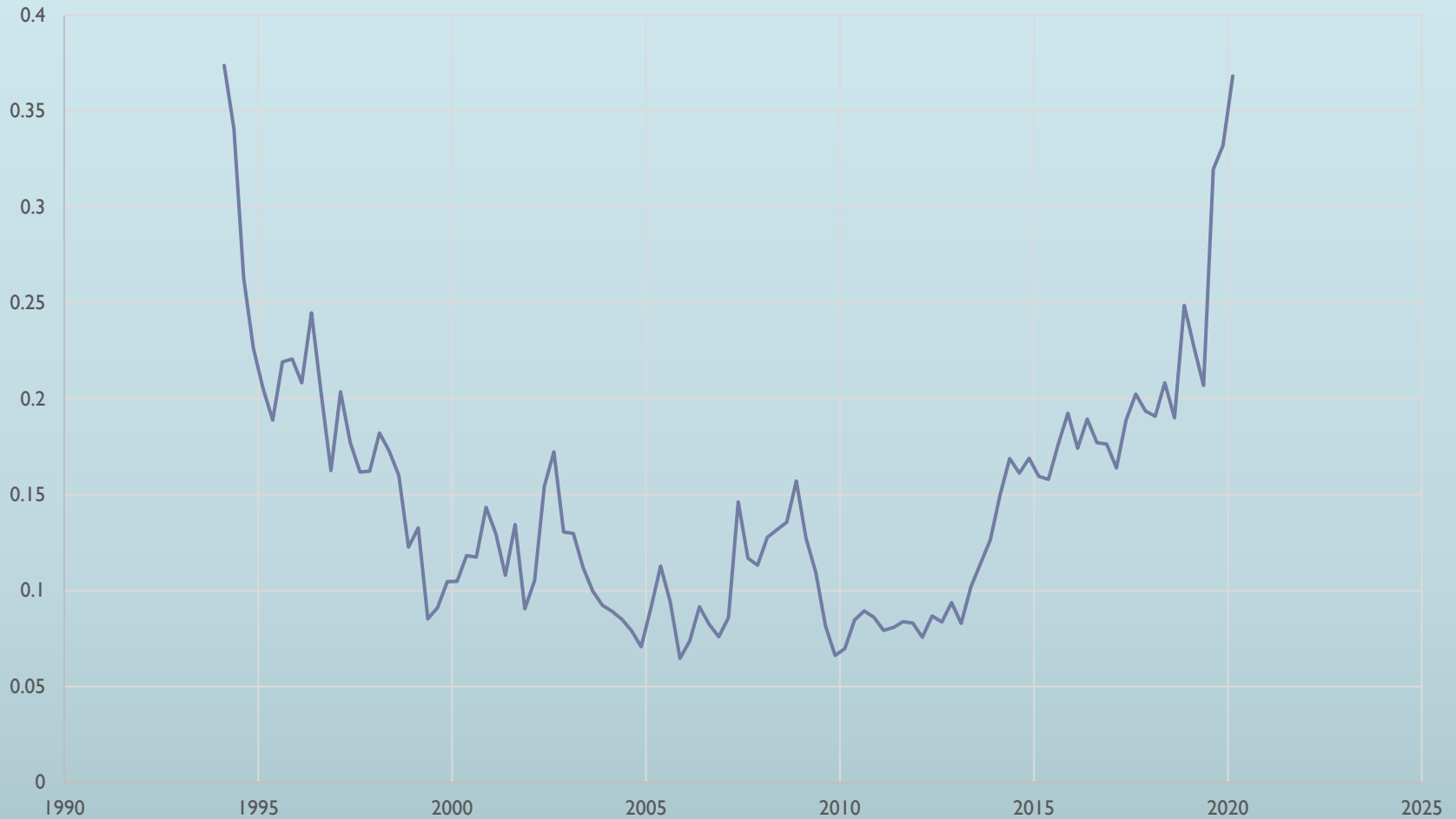
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# Do firms have leverage targets?

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IBM's leverage ratio



# A test

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- Consider the following model:

$$\left(\frac{D}{V}\right)_{t+1} = \gamma \left(\frac{D}{V}\right)^* + (1 - \gamma) \left(\frac{D}{V}\right)_t + \epsilon_{t+1}$$

where  $\epsilon$  is noise and  $\gamma$  is the speed of adjustment

- If firms have a target then  $\gamma$  should estimate to a number between 0 and 1
- The closer to 1 the faster the speed of adjustment
- IBM's  $\gamma$  estimates to around 0.08 but is not statistically significant at all conventional levels
- If one truncates the data at 2017,  $\gamma$  does become statistically significant
- See Python notebook



# A more reasonable test

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- $\left(\frac{D}{V}\right)^*$  probably varies over time as IBM's and market fundamentals do
- Hovakimian, Opler, and Titman (2001) and Strebulaev (2004), among many others, find evidence in favor of this view
- Dynamic trade-off theory



# Leverage and distress

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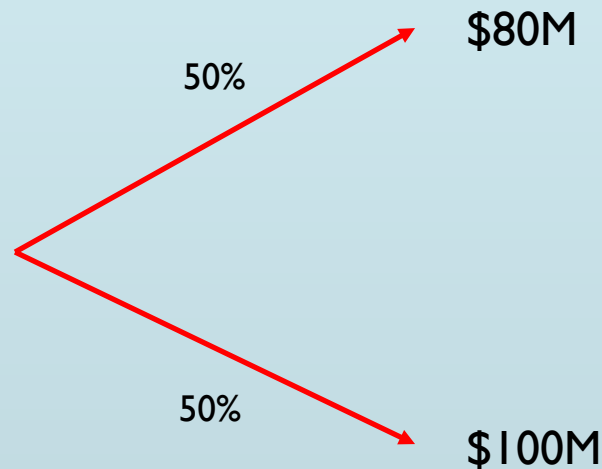
- *Debt overhang*: if new projects must be financed with new equity or junior debt, projects are passed up when their NPV falls short of the wealth transfer to senior debt holders (Myers, 1977)
- *Gambling for resurrection*: Limited liability caps shareholder losses, who cares about the downside? (Equivalently, equity is a call option on the firm's assets, the more volatility the better when default is a possibility)



# Debt overhang example

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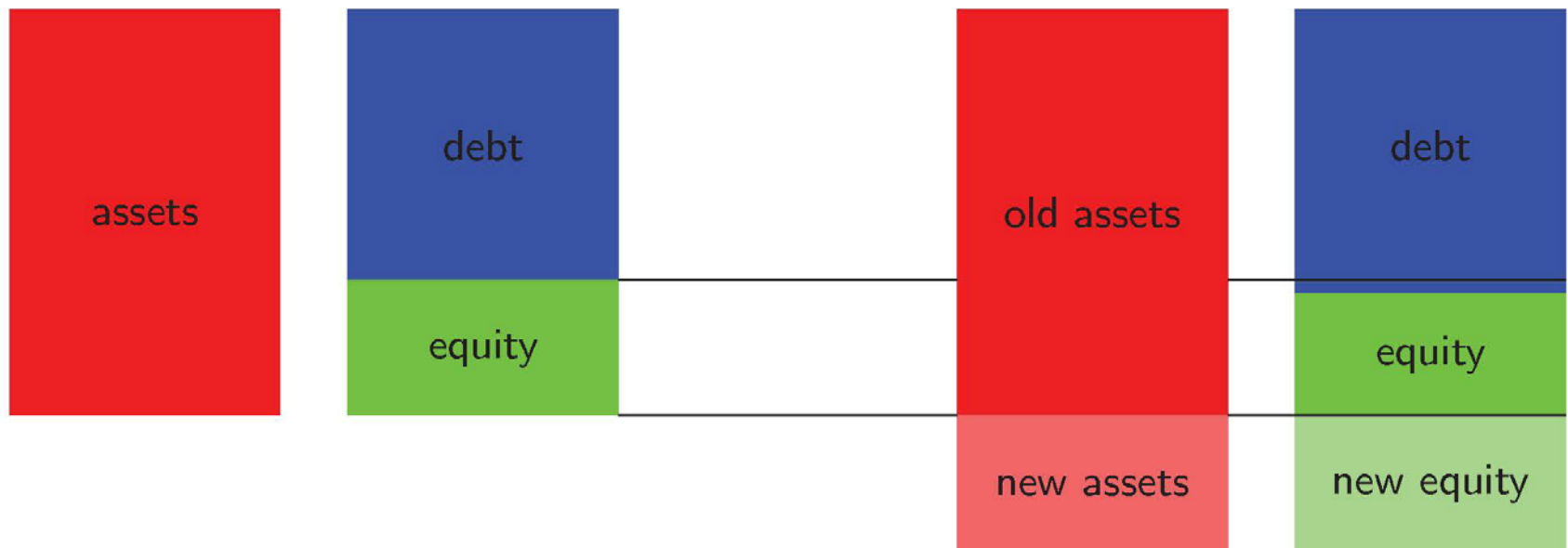
- Consider a corporation whose remaining cash flows are:



- Debt holders are owed \$90M in final period
  - A new project must be financed with equity, costs \$10M to implement and generates \$X for sure in the final period
  - As a stand alone project, equity investors would require a 5% return from this investment
  - But the project cannot be separated from the corporation
  - How high must X be to justify investing into the new project?
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# Conventional debt overhang



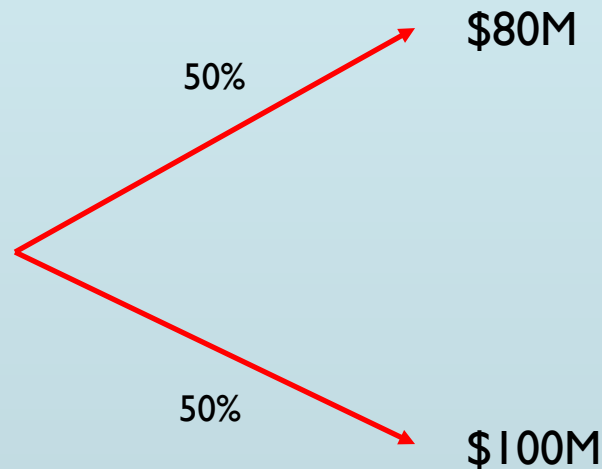
For shareholders to break even, the new assets must be purchased at a profit that exceeds the value transfer to creditors. (Myers, 1977)

Slide taken from Darell Duffie's Wisconsin talk on "Bank Debt Overhang and Financial Market Liquidity," hoping Darell won't mind

# Gambling for resurrection

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- Consider a corporation whose remaining cash flows are:



- Debt holders are owed **\$100M** in final period
  - A new project must be financed with equity, costs **\$0M** to implement and generate **\$10** in the final period in the good state, but **\$-1,000,000,000M** in the bad state
  - This is a positive NPV project for incumbent equity holders
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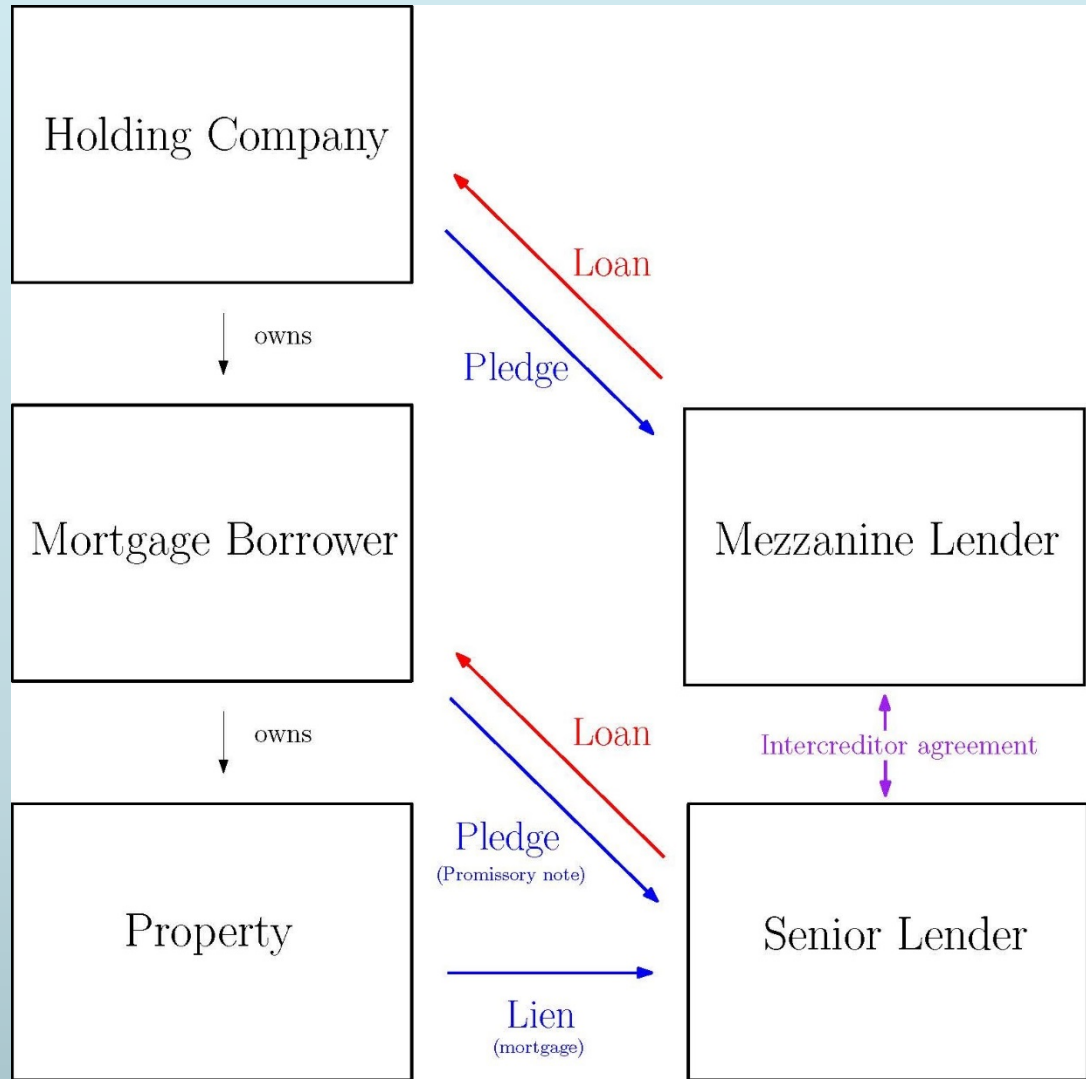
# Other consequences of capital policy

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- Debt reduces free cash flows hence moral hazard issues (Jensen, 1986)
- Debt is always there: low leverage means dry powder
- Secured vs unsecured debt: flexibility is valuable
- Debt holders bring skills to the table (monitoring, back-up operating skills...)



# A back-up QB view of mezzanine finance



# Pecking order (Myers and Majluf, 1984)

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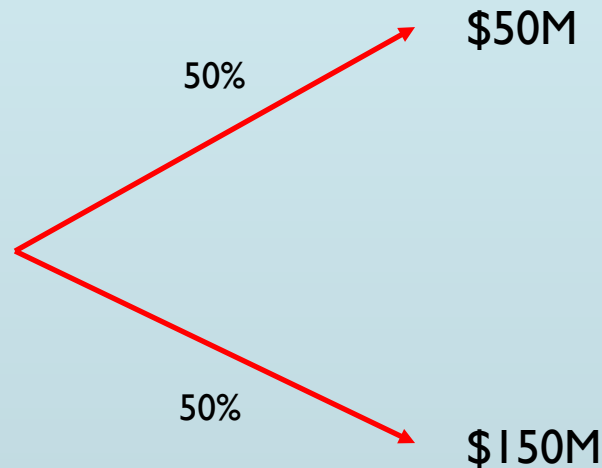
- According to this view, companies prefer raising funds in the following order:
  1. Internal funds
  2. Debt (safe, then risky, then hybrids)
  3. Equity
- “Good” firms don’t want to give away upside
- Firms/managers are more likely to issue equity when it is overvalued
- Raising external funds is costly



# Equity issuances signal bad news

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- Consider a corporation whose value next period, absent new investments, is:



- The corporation is and will remain unlevered
  - Investors are risk-neutral and do not discount the future
  - A new project yields payoff \$110M in the bad state and \$120M in the good state
  - It costs \$100M to implement today and requires fresh equity
  - Incumbent shareholders discover whether the state is good or bad prior to investing
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# No pooling equilibrium

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- Assume an equilibrium exists under which the project is implemented no matter what incumbent shareholders learn
- Value of the corporation today:

$$\frac{1}{2}(150 + 120) + \frac{1}{2}(50 + 110) = 215$$

- 100 has to be raised in new equity so incumbent's share is  $\frac{215-100}{215}$
- But incumbents who learn that the news is good are better off not investing since

$$150 > \frac{215 - 100}{215} \times 270$$

- The only possible equilibrium is one in which only incumbents who receive bad news invest
  - Intuition: incumbents with good news know that share is undervalued at investment time, dilution is too costly for them
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# Maturity management

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- A key aspect of capital structure management is the choice of a maturity structure in order to manage:
  1. Duration risk
  2. Refinancing/rollover risk
  
- In practice:
  1. ladders (no towers) are viewed as the prudent thing to do
  2. Average maturity should match average maturity of long-term investments (unless maturity transformation is your core business)



# Capital structure management in practice

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- Corporations, in some way or other, select a cost of capital (=debt rating) happy place given:
  1. Current and future investment opportunities
  2. Industry benchmarks
  
- Ratings, in turn, are a fairly well understood function of:
  1. Business risk
  2. Financial risk



# Financial risk management

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**Exhibit 1: Aggregate Metrics by Rating Category**

	Median			Median				
	Aaa-Aa	A	Baa	Ba	B	Caa-C	IG	SG
Interest Coverage	16.0	8.6	5.4	3.7	1.9	0.7	6.5	2.1
Asset Coverage	3.7	2.4	2.3	2.0	1.3	1.0	2.4	1.4
Leverage	31.6%	41.7%	44.8%	49.8%	68.7%	92.2%	43.6%	66.8%
Cash Flow-to-Debt	52.4%	32.6%	25.8%	21.6%	12.1%	6.4%	28.4%	12.7%
Return on Assets	11.6%	7.5%	5.3%	4.4%	1.7%	-2.1%	6.3%	1.9%
Profit	11.8%	9.0%	6.7%	5.0%	2.0%	-2.6%	7.8%	2.1%
Liquidity	7.8%	4.7%	4.0%	4.3%	3.9%	3.3%	4.6%	3.9%
Revenue Stability	7.2	7.3	6.1	5.2	6.1	7.3	6.6	5.9

Source: Moody's ratings and financial database as of July 1, 2006





## Appendix D Definition of Financial Metrics

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- Interest Coverage:
  - $(\text{EBIT} - \text{Interest Capitalized} + (1/3) * \text{Rental Expense}) / (\text{Interest Expense} + (1/3) * \text{Rental Expense} + \text{Preferred Dividends} / 0.65)$
- Asset Coverage:
  - $(\text{Total Assets} - \text{Goodwill} - \text{Intangibles}) / \text{Total Debt}$
- Leverage:
  - $(\text{Total Debt} + 8 * \text{Rental Expense}) / (\text{Total Debt} + 8 * \text{Rental Expense} + \text{Deferred Taxes} + \text{Minority Interest} + \text{Total Equity})$
- Cash Flow/Debt:
  - $(\text{Net After-Tax Income Before X-Items} + \text{Depreciations} - \text{Dividends}) / (\text{Total Debt} + 8 * \text{Rental Expense})$
- Return on Assets:
  - $\text{Net After-Tax Income Before X-Items} / 2 \text{ Year Average Assets}$
- Profit:
  - $\text{Net After-Tax Income Before X-Items} / \text{Net Sales}$
- Liquidity:
  - $\text{Cash \& Market Securities} / \text{Total Assets}$
- Revenue Stability:
  - $5 \text{ Year Average Net Sales} / 5 \text{ Year Standard Deviation Net Sales}$

# Merton's distance to default model

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- Merton models equity as a call option on the firm's assets (which it is given limited liability)
- Then (under strong assumptions) one shows “distance to default” to be

$$DD = \frac{\ln\left(\frac{V}{D}\right) + \left(r - \frac{\sigma^2}{2}\right) \times T}{\sigma \times \sqrt{T}}$$

where  $V$  is asset value,  $\sigma$  its volatility,  $T$  is debt maturity,  $r$  is the short-term interest rate

- Under even stronger assumptions, the probability of default is  $N(-DD)$



# Default probabilities implied by CDS spreads (1)

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- Assume constant hazard rates  $\lambda$ , constant recovery rate  $R$ , and flat CDS spreads  $\kappa$
- Then CDS spreads  $\kappa$  should solve:

$$\lambda = \frac{\kappa}{1 - R}$$

- Further, letting  $P(0, t)$  be probability of default between now and time  $t$ :

$$P(0, t) = \int_0^t (1 - P(0, s))\lambda ds$$



# Default probabilities implied by CDS spreads (2)

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- It follows that  $\frac{dP(0,t)}{dt} = (1 - P(0,t))\lambda$
- This is a first-order differential equation whose solution, given  $P(0,0) = 0$  is:

$$P(0,t) = 1 - e^{-\lambda t}$$

- So, finally,

$$P(0,t) = 1 - e^{-\frac{\kappa t}{1-R}}$$

