



# The value of flexibility



Corporate Finance

# Optionality matters

---

- Most corporate decisions come with a lot of flexibility, i.e. the option to adjust as more information arises
- Most investment projects have option-like aspects: develop (call), expand (call), upgrade (call), contract (put), abandon (put)...
- These real options account for a significant part of value
- In well functioning markets where NPVs on activated projects should not be too far from zero, investments only make sense if and when the value of those options is properly measured



# Example

---

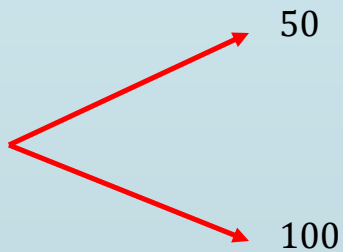
- Consider an investment project whose continuation value at date 1 is either  $100M$  or  $50M$
  - It can be activated in two distinct locations
  - In location 1, there is no exit strategy and you are stuck with the project
  - In location 2, the project can be scrapped for  $60M$  (instead of begin continued and upon discovering continuation value)
  - Project 2 = Project 1 project + option to scrap
  - $NPV(\text{project 2}) = NPV(\text{project 1}) + \text{value of option to scrap}$
  - Assume the market value of the location 1 project is  $70M$
  - Risk-free rate is 5%
  - What is the value of the option to scrap? What is the value of location 2 project?
- 



# Replication

---

**Project**



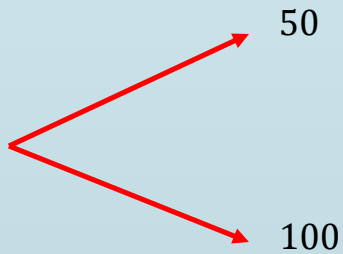
1. Invest  $\$a$  at risk free rate and buy fraction  $x$  of project 1
2. Set  $a$  and  $x$  so that option to scrap and replicating portfolio have the same payoff
3. Value of option is  $a + 70x$ , by the law of one price



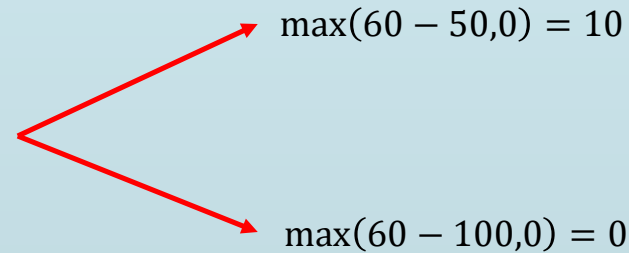
# Replication

---

**Project**



**Option to scrap**

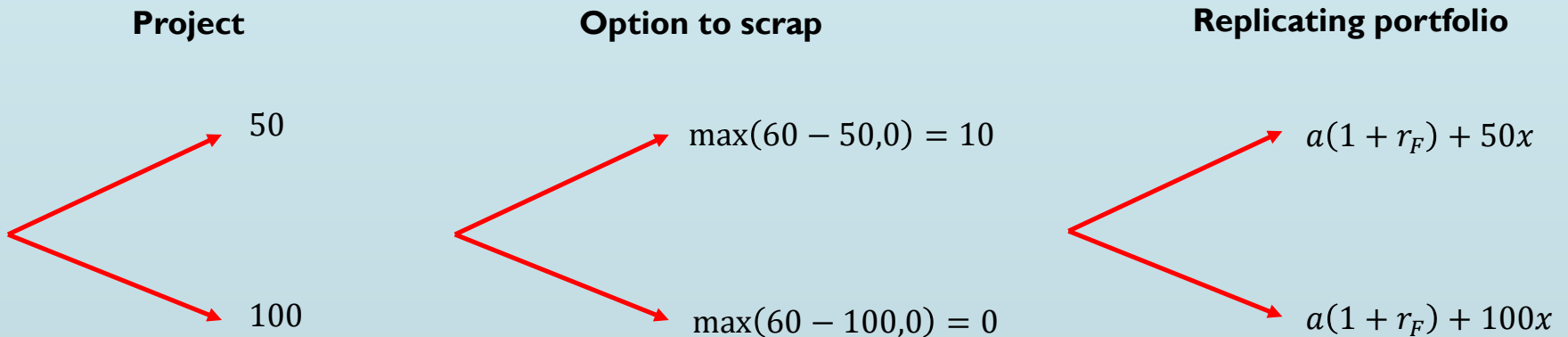


1. Invest  $\$a$  at risk free rate and buy fraction  $x$  of project 1
2. Set  $a$  and  $x$  so that option to scrap and replicating portfolio have the same payoff
3. Value of option is  $a + 70x$ , by the law of one price



# Replication

---



1. Invest  $\$a$  at risk free rate and buy fraction  $x$  of project 1
2. Set  $a$  and  $x$  so that option to scrap and replicating portfolio have the same payoff
3. Value of option is  $a + 70x$ , by the law of one price



## Example 2: the option to delay refinancing

---

- Return to the refi problem from chapter 1
- A corporation has the option to prepay (*call*) a bond with 5 years to maturity, \$100M in remaining principal, a 10% yearly rate, fixed and monthly payments
- It can replace it with a 5 year bond with the same payment structure but a 9% yearly rate
- Prepayment penalties are 2% of outstanding principal
- “Tomorrow,” rates will be either 8.5% or 9.5%
- Should Risk free rate between today and tomorrow is 0.005%
- Should the company wait to refinance?



# Why not do both?

---

- If you refi today, refinancing again tomorrow to go from 9% to 8.5% will not make sense because the increment won't justify bearing the cost
- Exercising the option today, kills the option to exercise it tomorrow
- That is a cost (an opportunity cost)
- So we should exercise only if  $PV(\text{refi})$  exceeds refi cost plus the value of the option we killed

